

t7\_tex\_1 (TM-  
Mdko7QPnqYf9WYMXsXcRMpbLbdQukZiNw)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_pre\_topc : \iota \Rightarrow o$  be given. Let  $l1\_pre\_topc : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k6\_tmap\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r1\_tarski : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v2\_tops\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v3\_tops\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_pre\_topc : \iota \Rightarrow \iota$  be given. Let  $k5\_tmap\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v4\_pre\_topc : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_pre\_topc : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v2\_pre\_topc X0) \wedge (l1\_pre\_topc \\ & X0))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 \\ & X0))) \Rightarrow ((u1\_struct\_0 (k6\_tmap\_1 X0 X1) = u1\_struct\_0 X0) \wedge (u1\_pre\_topc \\ & (k6\_tmap\_1 X0 X1) = k5\_tmap\_1 X0 X1))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v2\_pre\_topc X0) \wedge (l1\_pre\_topc \\ & X0))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 \\ & X0))) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 (u1\_struct\_0 \\ & (k6\_tmap\_1 X0 (k3\_subset\_1 (u1\_struct\_0 X0) X1)))))) \Rightarrow (((X2 = X1) \wedge \\ & (v2\_tops\_1 X1 X0)) \Rightarrow ((v2\_tops\_1 X2 (k6\_tmap\_1 X0 (k3\_subset\_1 ( \\ & u1\_struct\_0 X0) X1))) \wedge (v4\_pre\_topc X2 (k6\_tmap\_1 X0 (k3\_subset\_1 \\ & (u1\_struct\_0 X0) X1)))))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v2\_pre\_topc X0) \wedge (l1\_pre\_topc \\ & X0))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 \\ & X0))) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 (u1\_struct\_0 \\ & X0))) \Rightarrow (((v3\_tops\_1 X1 X0) \wedge (r1\_tarski X2 X1)) \Rightarrow (v3\_tops\_1 X2 X0)))) \end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(((\neg v2\_struct\_0 X0)\wedge((v2\_pre\_topc X0)\wedge \\ & (l1\_pre\_topc X0)))\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 \\ & X0))))\Rightarrow((\neg v2\_struct\_0 (k6\_tmap\_1 X0 X1))\wedge((v1\_pre\_topc (k6\_tmap\_1 \\ & X0 X1))\wedge(v2\_pre\_topc (k6\_tmap\_1 X0 X1)))) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(((\neg v2\_struct\_0 X0)\wedge((v2\_pre\_topc X0)\wedge \\ & (l1\_pre\_topc X0)))\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 \\ & X0))))\Rightarrow((v1\_pre\_topc (k6\_tmap\_1 X0 X1))\wedge((v2\_pre\_topc (k6\_tmap\_1 \\ & X0 X1))\wedge(l1\_pre\_topc (k6\_tmap\_1 X0 X1)))) \end{aligned} \quad (5)$$

Assume the following.

$$\forall X0.\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 X0))\Rightarrow(m1\_subset\_1 (k3\_subset\_1 X0 X1) (k1\_zfmisc\_1 X0)) \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v2\_pre\_topc X0)\wedge(l1\_pre\_topc X0))\Rightarrow(\forall X1. \\ & (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))\Rightarrow(((v4\_pre\_topc \\ & X1 X0)\wedge(v2\_tops\_1 X1 X0))\Rightarrow(v3\_tops\_1 X1 X0))) \end{aligned} \quad (7)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0)\wedge((v2\_pre\_topc X0)\wedge(l1\_pre\_topc \\ & X0)))\Rightarrow(\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 \\ & X0)))\Rightarrow(\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 (u1\_struct\_0 \\ & (k6\_tmap\_1 X0 (k3\_subset\_1 (u1\_struct\_0 X0) X1))))\Rightarrow(((r1\_tarski \\ & X2 X1)\wedge(v2\_tops\_1 X1 X0))\Rightarrow(v3\_tops\_1 X2 (k6\_tmap\_1 X0 (k3\_subset\_1 \\ & (u1\_struct\_0 X0) X1)))))) \end{aligned}$$