

t81\_exchsort  
(TMUfC99SdmTd3FqrRpa2FHvfHQAEkZ3HKBq)

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Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_finset\_1 : \iota \Rightarrow o$  be given. Let  $v1\_exchsort : \iota \Rightarrow o$  be given. Let  $v2\_exchsort : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_xboole\_0 : \iota$  be given. Let  $k4\_exchsort : \iota \Rightarrow \iota$  be given. Let  $k1\_ordinal4 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_afinsq\_1 : \iota \Rightarrow \iota$  be given. Let  $v5\_ordinal1 : \iota \Rightarrow o$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_afinsq\_1 : \iota \Rightarrow \iota$  be given. Let  $v3\_ordinal1 : \iota \Rightarrow o$  be given. Let  $k10\_ordinal2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $k1\_ordinal1 : \iota \Rightarrow \iota$  be given. Let  $k3\_tarski : \iota \Rightarrow \iota$  be given. Let  $k6\_numbers : \iota$  be given. Let  $k3\_afinsq\_1 : \iota \Rightarrow \iota$  be given. Let  $k1\_card\_1 : \iota \Rightarrow \iota$  be given. Let  $k9\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $v7\_ordinal1 : \iota \Rightarrow o$  be given. Let  $k2\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_tarski : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0. \forall X1. ((v1\_relat\_1 X1) \wedge ((v5\_ordinal1 X1) \wedge ((v1\_funct\_1 X1) \wedge (v1\_finset\_1 X1)))) \Rightarrow (k1\_funct\_1 (k1\_ordinal4 X1 (k5\_afinsq\_1 X0)) (k1\_afinsq\_1 X1) = X0) \quad (1)$$

Assume the following.

$$\forall X0. (v3\_ordinal1 X0) \Rightarrow (k10\_ordinal2 X0 np\_1 = k1\_ordinal1 X0) \quad (2)$$

Assume the following.

$$\forall X0. (v3\_ordinal1 X0) \Rightarrow (k3\_tarski (k1\_ordinal1 X0) = X0) \quad (3)$$

Assume the following.

$$k6\_numbers = k1\_xboole\_0 \quad (4)$$

Assume the following.

$$\forall X0. k5\_afinsq\_1 X0 = k3\_afinsq\_1 X0 \quad (5)$$

Assume the following.

$$\forall X0. ((v1\_relat\_1 X0) \wedge ((v5\_ordinal1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v1\_finset\_1 X0)))) \Rightarrow (k1\_afinsq\_1 X0 = k1\_card\_1 X0) \quad (6)$$

Assume the following.

$$\forall X0.((v1\_relat\_1 X0) \wedge ((v5\_ordinal1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v1\_finset\_1 X0)))) \Rightarrow (k1\_card\_1 X0 = k9\_xtuple\_0 X0) \quad (7)$$

Assume the following.

$$\forall X0.(v5\_ordinal1 (k3\_afinsq\_1 X0)) \wedge (v1\_finset\_1 (k3\_afinsq\_1 X0)) \quad (8)$$

Assume the following.

$$\forall X0.((v1\_relat\_1 X0) \wedge ((v5\_ordinal1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v1\_finset\_1 X0)))) \Rightarrow (v7\_ordinal1 (k9\_xtuple\_0 X0)) \quad (9)$$

Assume the following.

$$\forall X0.(v1\_relat\_1 (k5\_afinsq\_1 X0)) \wedge (v1\_funct\_1 (k5\_afinsq\_1 X0)) \quad (10)$$

Assume the following.

$$\forall X0.\forall X1.(((v1\_relat\_1 X0) \wedge ((v5\_ordinal1 X0) \wedge (v1\_funct\_1 X0))) \wedge ((v1\_relat\_1 X1) \wedge ((v5\_ordinal1 X1) \wedge (v1\_funct\_1 X1)))) \Rightarrow ((v1\_relat\_1 (k1\_ordinal4 X0 X1)) \wedge ((v5\_ordinal1 (k1\_ordinal4 X0 X1)) \wedge (v1\_funct\_1 (k1\_ordinal4 X0 X1)))) \quad (11)$$

Assume the following.

$$\forall X0.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v1\_exchsort X0))) \Rightarrow (k4\_exchsort X0 = k1\_funct\_1 X0 (k3\_tarski (k9\_xtuple\_0 X0))) \quad (12)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_relat\_1 X1) \wedge (v1\_funct\_1 X1)) \Rightarrow ((X1 = k5\_afinsq\_1 X0) \Leftrightarrow ((k9\_xtuple\_0 X1 = np\_1) \wedge (k1\_funct\_1 X1 k6\_numbers = X0))) \quad (13)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1\_relat\_1 X0) \wedge ((v5\_ordinal1 X0) \wedge (v1\_funct\_1 X0))) \Rightarrow \\ & (\forall X1.((v1\_relat\_1 X1) \wedge ((v5\_ordinal1 X1) \wedge (v1\_funct\_1 X1))) \Rightarrow (\forall X2.((v1\_relat\_1 X2) \wedge ((v5\_ordinal1 X2) \wedge (v1\_funct\_1 X2)))) \Rightarrow ((X2 = k1\_ordinal4 X0 X1) \Leftrightarrow ((k9\_xtuple\_0 X2 = k10\_ordinal2 (k9\_xtuple\_0 X0) (k9\_xtuple\_0 X1)) \wedge ((\forall X3.(v3\_ordinal1 X3) \Rightarrow ((X3 \in k9\_xtuple\_0 X0) \Rightarrow (k1\_funct\_1 X2 X3 = k1\_funct\_1 X0 X3)))) \wedge ((\forall X3.(v3\_ordinal1 X3) \Rightarrow ((X3 \in k9\_xtuple\_0 X1) \Rightarrow (k1\_funct\_1 X2 (k10\_ordinal2 (k9\_xtuple\_0 X0) X3) = k1\_funct\_1 X1 X3)))))) \wedge \\ & (14) \end{aligned}$$

Assume the following.

$$\forall X0.k1\_ordinal1\ X0 = k2\_xboole\_0\ X0\ (k1\_tarski\ X0) \quad (15)$$

Assume the following.

$$\forall X0.((v1\_relat\_1\ X0)\wedge((v1\_funct\_1\ X0)\wedge((v1\_exhsort\ X0)\wedge(v2\_exhsort\ X0\ k1\_xboole\_0))))\Rightarrow((v5\_ordinal1\ X0)\wedge((v1\_relat\_1\ X0)\wedge((v1\_funct\_1\ X0)\wedge(v1\_exhsort\ X0)))) \quad (16)$$

Assume the following.

$$\forall X0.(v7\_ordinal1\ X0)\Rightarrow((v3\_ordinal1\ X0)\wedge(v7\_ordinal1\ X0)) \quad (17)$$

Assume the following.

$$\forall X0.((v5\_ordinal1\ X0)\wedge((v1\_relat\_1\ X0)\wedge(v1\_funct\_1\ X0)))\Rightarrow((v1\_relat\_1\ X0)\wedge((v1\_funct\_1\ X0)\wedge(v1\_exhsort\ X0))) \quad (18)$$

**Theorem 1**

$$\forall X0.\forall X1.((v1\_relat\_1\ X1)\wedge((v1\_funct\_1\ X1)\wedge((v1\_finset\_1\ X1)\wedge((v1\_exhsort\ X1)\wedge(v2\_exhsort\ X1\ k1\_xboole\_0))))))\Rightarrow(k4\_exhsort\ (k1\_ordinal4\ X1\ (k5\_afinsq\_1\ X0)) = X0)$$