

t84\_funct\_1  
(TMVt8SCvE76z9gHKUcQdG9FutXvHfJw4t7p)

October 27, 2020

Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v2\_funct\_1 : \iota \Rightarrow o$  be given. Let  $k7\_relat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k8\_relat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_funct\_1 : \iota \Rightarrow \iota$  be given. Let  $k4\_relat\_1 : \iota \Rightarrow \iota$  be given. Let  $k3\_relat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k10\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $k9\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0. k2\_funct\_1 (k4\_relat\_1 X0) = k4\_relat\_1 X0 \quad (1)$$

Assume the following.

$$\forall X0. ((v1\_relat\_1 X0) \wedge (v1\_funct\_1 X0)) \Rightarrow (\forall X1. ((v1\_relat\_1 X1) \wedge (v1\_funct\_1 X1)) \Rightarrow (((v2\_funct\_1 X0) \wedge (v2\_funct\_1 X1)) \Rightarrow (k2\_funct\_1 (k3\_relat\_1 X0 X1) = k3\_relat\_1 (k2\_funct\_1 X1) (k2\_funct\_1 X0)))) \quad (2)$$

Assume the following.

$$\forall X0. ((v1\_relat\_1 X0) \wedge (v1\_funct\_1 X0)) \Rightarrow ((v2\_funct\_1 X0) \Rightarrow ((k10\_xtuple\_0 X0 = k9\_xtuple\_0 (k2\_funct\_1 X0)) \wedge (k9\_xtuple\_0 X0 = k10\_xtuple\_0 (k2\_funct\_1 X0)))) \quad (3)$$

Assume the following.

$$\forall X0. (v1\_relat\_1 X0) \Rightarrow (\forall X1. (v1\_relat\_1 X1) \Rightarrow (k9\_xtuple\_0 (k3\_relat\_1 X0 X1) = k8\_relat\_1 X0 (k9\_xtuple\_0 X1))) \quad (4)$$

Assume the following.

$$\forall X0. (v1\_relat\_1 X0) \Rightarrow (\forall X1. (v1\_relat\_1 X1) \Rightarrow (k10\_xtuple\_0 (k3\_relat\_1 X0 X1) = k7\_relat\_1 X1 (k10\_xtuple\_0 X0))) \quad (5)$$

Assume the following.

$$\forall X0. k10\_xtuple\_0 (k4\_relat\_1 X0) = X0 \quad (6)$$

Assume the following.

$$\forall X0.k9\_xtuple\_0 (k4\_relat\_1 X0) = X0 \quad (7)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.(((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge(v2\_funct\_1 \\ X0)))\wedge((v1\_relat\_1 X1)\wedge((v1\_funct\_1 X1)\wedge(v2\_funct\_1 X1))))\Rightarrow \\ ((v1\_relat\_1 (k3\_relat\_1 X0 X1))\wedge(v2\_funct\_1 (k3\_relat\_1 X0 X1))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge(v2\_funct\_1 X0)))\Rightarrow \\ ((v1\_relat\_1 (k2\_funct\_1 X0))\wedge((v1\_funct\_1 (k2\_funct\_1 X0))\wedge \\ (v2\_funct\_1 (k2\_funct\_1 X0)))) \end{aligned} \quad (9)$$

Assume the following.

$$\forall X0.(v1\_relat\_1 (k4\_relat\_1 X0))\wedge(v2\_funct\_1 (k4\_relat\_1 X0)) \quad (10)$$

Assume the following.

$$\forall X0.(v1\_relat\_1 (k4\_relat\_1 X0))\wedge(v1\_funct\_1 (k4\_relat\_1 X0)) \quad (11)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.(((v1\_relat\_1 X0)\wedge(v1\_funct\_1 X0))\wedge(( \\ v1\_relat\_1 X1)\wedge(v1\_funct\_1 X1)))\Rightarrow((v1\_relat\_1 (k3\_relat\_1 X0 \\ X1))\wedge(v1\_funct\_1 (k3\_relat\_1 X0 X1))) \end{aligned} \quad (12)$$

Assume the following.

$$\forall X0.v1\_relat\_1 (k4\_relat\_1 X0) \quad (13)$$

Assume the following.

$$\forall X0.\forall X1.v1\_relat\_1 (k3\_relat\_1 X0 X1) \quad (14)$$

**Theorem 1**

$$\begin{aligned} \forall X0.\forall X1.((v1\_relat\_1 X1)\wedge(v1\_funct\_1 X1))\Rightarrow((v2\_funct\_1 \\ X1)\Rightarrow(k7\_relat\_1 X1 X0 = k8\_relat\_1 (k2\_funct\_1 X1) X0)) \end{aligned}$$