

# t8\_cat\_4 (TMSwppt- gyX6MUAf6KioyrZGi7UQtX2rMWVJ)

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Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k5\_cat\_4 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v10\_cat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u4\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v11\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v3\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v5\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v6\_cat\_1 : \iota \Rightarrow o$  be given. Let  $l1\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v9\_cat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k4\_cat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v2\_cat\_4 : \iota \Rightarrow o$  be given. Let  $m1\_cat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l1\_cat\_4 : \iota \Rightarrow o$  be given. Let  $k2\_cat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_xboole\_0 : \iota$  be given. Let  $k5\_cat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (m1\_subset\_1 X2 (u4\_struct\_0 \\ & (k5\_cat\_4 X0 X1))) \Rightarrow (\forall X3. (m1\_subset\_1 X3 (u4\_struct\_0 ( \\ & k5\_cat\_4 X0 X1))) \Rightarrow (X2 = X3)) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_cat\_1 \\ & X0) \wedge ((v3\_cat\_1 X0) \wedge ((v4\_cat\_1 X0) \wedge ((v5\_cat\_1 X0) \wedge ((v6\_cat\_1 \\ & X0) \wedge (l1\_cat\_1 X0)))))))) \Rightarrow (\forall X1. (m1\_subset\_1 X1 (u1\_struct\_0 \\ & X0)) \Rightarrow (v9\_cat\_1 (k4\_cat\_1 X0 X1) X0 X1 X1)) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (m1\_subset\_1 X2 (u1\_struct\_0 \\ & (k5\_cat\_4 X0 X1))) \Rightarrow (\forall X3. (m1\_subset\_1 X3 (u1\_struct\_0 ( \\ & k5\_cat\_4 X0 X1))) \Rightarrow (X2 = X3)) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. (\neg v2\_struct\_0 (k5\_cat\_4 X0 X1)) \wedge ((\neg v11\_struct\_0 \\ & (k5\_cat\_4 X0 X1)) \wedge ((v2\_cat\_1 (k5\_cat\_4 X0 X1)) \wedge ((v3\_cat\_1 (k5\_cat\_4 \\ & X0 X1)) \wedge ((v4\_cat\_1 (k5\_cat\_4 X0 X1)) \wedge ((v5\_cat\_1 (k5\_cat\_4 X0 X1)) \wedge \\ & ((v6\_cat\_1 (k5\_cat\_4 X0 X1)) \wedge (v2\_cat\_4 (k5\_cat\_4 X0 X1)))))))) \end{aligned} \quad (4)$$

Assume the following.

$$\forall X0.\exists X1.m1\_subset\_1 X1 X0 \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v2\_struct\_0 X0)\wedge((\neg v11\_struct\_0 \\ & X0)\wedge(l1\_cat\_1 X0)))\wedge((m1\_subset\_1 X1 (u1\_struct\_0 X0))\wedge(m1\_subset\_1 \\ & X2 (u1\_struct\_0 X0))))\Rightarrow(\forall X3.(m1\_cat\_1 X3 X0 X1 X2)\Rightarrow(m1\_subset\_1 \\ & X3 (u4\_struct\_0 X0))) \end{aligned} \quad (6)$$

Assume the following.

$$\forall X0.(l1\_cat\_4 X0)\Rightarrow(l1\_cat\_1 X0) \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.(v2\_cat\_4 (k5\_cat\_4 X0 X1))\wedge(l1\_cat\_4 (k5\_cat\_4 X0 X1)) \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(((\neg v2\_struct\_0 X0)\wedge((\neg v11\_struct\_0 X0)\wedge \\ & ((v5\_cat\_1 X0)\wedge((v6\_cat\_1 X0)\wedge(l1\_cat\_1 X0))))\wedge(m1\_subset\_1 \\ & X1 (u1\_struct\_0 X0)))\Rightarrow(m1\_cat\_1 (k4\_cat\_1 X0 X1) X0 X1 X1) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} & \forall X0.(((\neg v2\_struct\_0 X0)\wedge((\neg v11\_struct\_0 X0)\wedge((v2\_cat\_1 \\ & X0)\wedge((v3\_cat\_1 X0)\wedge((v4\_cat\_1 X0)\wedge((v5\_cat\_1 X0)\wedge((v6\_cat\_1 \\ & X0)\wedge(l1\_cat\_1 X0))))))))\Rightarrow(\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 \\ & X0))\Rightarrow((v10\_cat\_1 X1 X0)\Leftrightarrow(\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 \\ & X0))\Rightarrow((k2\_cat\_1 X0 X2 X1\neq k1\_xboole\_0)\wedge(\exists X3.(m1\_cat\_1 \\ & X3 X0 X2 X1)\wedge(\forall X4.(m1\_cat\_1 X4 X0 X2 X1)\Rightarrow(X3 = X4)))))) \end{aligned} \quad (10)$$

Assume the following.

$$\begin{aligned} & \forall X0.(((\neg v2\_struct\_0 X0)\wedge((\neg v11\_struct\_0 X0)\wedge((v2\_cat\_1 \\ & X0)\wedge((v3\_cat\_1 X0)\wedge((v4\_cat\_1 X0)\wedge((v5\_cat\_1 X0)\wedge((v6\_cat\_1 \\ & X0)\wedge(l1\_cat\_1 X0))))))))\Rightarrow(\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 \\ & X0))\Rightarrow(\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 X0))\Rightarrow(\forall X3. \\ & (m1\_cat\_1 X3 X0 X1 X2)\Rightarrow((v9\_cat\_1 X3 X0 X1 X2)\Leftrightarrow((k2\_cat\_1 X0 X1 X2\neq \\ & k1\_xboole\_0)\wedge((k2\_cat\_1 X0 X2 X1\neq k1\_xboole\_0)\wedge(\exists X4.( \\ & m1\_cat\_1 X4 X0 X2 X1)\wedge((k5\_cat\_1 X0 X2 X1 X2 X4 X3 = k4\_cat\_1 X0 X2)\wedge \\ & (k5\_cat\_1 X0 X1 X2 X1 X3 X4 = k4\_cat\_1 X0 X1)))))))) \end{aligned} \quad (11)$$

**Theorem 1**

$$\forall X0.\forall X1.\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 (k5\_cat\_4 X0 X1)))\Rightarrow(v10\_cat\_1 X2 (k5\_cat\_4 X0 X1))$$