

t8\_osalg\_1 (TML-  
SnW4Woo8wEj1yVXfuEE6zau93K3NpzxD)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v11\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v4\_osalg\_1 : \iota \Rightarrow o$  be given. Let  $v5\_osalg\_1 : \iota \Rightarrow o$  be given. Let  $l3\_osalg\_1 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u4\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $v1\_orders\_3 : \iota \Rightarrow o$  be given. Let  $r1\_osalg\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r2\_osalg\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r3\_orders\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v3\_orders\_2 : \iota \Rightarrow o$  be given. Let  $v4\_orders\_2 : \iota \Rightarrow o$  be given. Let  $v5\_orders\_2 : \iota \Rightarrow o$  be given. Let  $l1\_orders\_2 : \iota \Rightarrow o$  be given. Let  $m2\_finseq\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k3\_finseq\_2 : \iota \Rightarrow \iota$  be given. Let  $r1\_orders\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l1\_osalg\_1 : \iota \Rightarrow o$  be given. Let  $l2\_osalg\_1 : \iota \Rightarrow o$  be given. Let  $l1\_msualg\_1 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v3\_orders\_2 X0) \wedge ((v4\_orders\_2 \\ & X0) \wedge ((v5\_orders\_2 X0) \wedge (l1\_orders\_2 X0)))) \Rightarrow (\forall X1.(m2\_finseq\_2 \\ & X1 (u1\_struct\_0 X0) (k3\_finseq\_2 (u1\_struct\_0 X0))) \Rightarrow (\forall X2. \\ & (m2\_finseq\_2 X2 (u1\_struct\_0 X0) (k3\_finseq\_2 (u1\_struct\_0 X0))) \Rightarrow \\ & ((v1\_orders\_3 X0) \wedge (r2\_osalg\_1 X0 X1 X2)) \Rightarrow (X1 = X2)))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v1\_orders\_3 X0) \wedge (l1\_orders\_2 \\ & X0))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2. \\ & (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow ((r1\_orders\_2 X0 X1 X2) \Leftrightarrow (X1 = \\ & X2)))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (((\neg v2\_struct\_0 X0) \wedge ((v3\_orders\_2 \\ & X0) \wedge (l1\_orders\_2 X0))) \wedge ((m1\_subset\_1 X1 (u1\_struct\_0 X0)) \wedge \\ & m1\_subset\_1 X2 (u1\_struct\_0 X0))) \Rightarrow ((r3\_orders\_2 X0 X1 X2) \Leftrightarrow (r1\_orders\_2 \\ & X0 X1 X2)) \end{aligned} \quad (3)$$

Assume the following.

$$\forall X0.(l3\_osalg\_1 X0) \Rightarrow ((l1\_osalg\_1 X0) \wedge (l2\_osalg\_1 X0)) \quad (4)$$

Assume the following.

$$\forall X0.(l2\_osalg\_1 X0) \Rightarrow ((l1\_msualg\_1 X0) \wedge (l1\_orders\_2 X0)) \quad (5)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. (((\neg v2\_struct\_0 X0) \wedge (\neg v11\_struct\_0 X0) \wedge \\ (l1\_msualg\_1 X0)) \wedge (m1\_subset\_1 X1 (u4\_struct\_0 X0))) \Rightarrow (m1\_subset\_1 \\ (k2\_msualg\_1 X0 X1) (u1\_struct\_0 X0)) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. (((\neg v2\_struct\_0 X0) \wedge (\neg v11\_struct\_0 X0) \wedge \\ (l1\_msualg\_1 X0)) \wedge (m1\_subset\_1 X1 (u4\_struct\_0 X0))) \Rightarrow (m2\_finseq\_2 \\ (k1\_msualg\_1 X0 X1) (u1\_struct\_0 X0) (k3\_finseq\_2 (u1\_struct\_0 \\ X0))) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} \forall X0. ((\neg v2\_struct\_0 X0) \wedge (\neg v11\_struct\_0 X0) \wedge (l1\_osalg\_1 \\ X0)) \Rightarrow ((v5\_osalg\_1 X0) \Leftrightarrow (\forall X1. (m1\_subset\_1 X1 (u4\_struct\_0 \\ X0)) \Rightarrow (\forall X2. (m1\_subset\_1 X2 (u4\_struct\_0 X0)) \Rightarrow (((r1\_osalg\_1 \\ X0 X1 X2) \wedge ((k1\_msualg\_1 X0 X1 = k1\_msualg\_1 X0 X2) \wedge (k2\_msualg\_1 \\ X0 X1 = k2\_msualg\_1 X0 X2)))) \Rightarrow (X1 = X2)))))) \end{aligned} \quad (8)$$

Assume the following.

$$\forall X0.(l3\_osalg\_1 X0) \Rightarrow ((v4\_osalg\_1 X0) \Rightarrow ((v3\_orders\_2 X0) \wedge \\ ((v4\_orders\_2 X0) \wedge (v5\_orders\_2 X0)))) \quad (9)$$

**Theorem 1**

$$\begin{aligned} \forall X0. ((\neg v2\_struct\_0 X0) \wedge (\neg v11\_struct\_0 X0) \wedge ((v4\_osalg\_1 \\ X0) \wedge ((v5\_osalg\_1 X0) \wedge (l3\_osalg\_1 X0)))) \Rightarrow (\forall X1. (m1\_subset\_1 \\ X1 (u4\_struct\_0 X0)) \Rightarrow (\forall X2. (m1\_subset\_1 X2 (u4\_struct\_0 \\ X0)) \Rightarrow (((v1\_orders\_3 X0) \wedge ((r1\_osalg\_1 X0 X1 X2) \wedge ((r2\_osalg\_1 \\ X0 (k1\_msualg\_1 X0 X1) (k1\_msualg\_1 X0 X2)) \wedge (r3\_orders\_2 X0 (k2\_msualg\_1 \\ X0 X1) (k2\_msualg\_1 X0 X2)))))) \Rightarrow (X1 = X2)))))) \end{aligned}$$