

## t8\_topmetr3

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Let  $v1\_xreal\_0 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $k1\_numbers : \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k2\_topmetr : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_xxreal\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v2\_comseq\_2 : \iota \Rightarrow o$  be given. Let  $v2\_tbsp\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_seq\_2 : \iota \Rightarrow \iota$  be given. Let  $k1\_tbsp\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k8\_metric\_1 : \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_metric\_1 : \iota \Rightarrow o$  be given. Let  $v6\_metric\_1 : \iota \Rightarrow o$  be given. Let  $v7\_metric\_1 : \iota \Rightarrow o$  be given. Let  $v8\_metric\_1 : \iota \Rightarrow o$  be given. Let  $v9\_metric\_1 : \iota \Rightarrow o$  be given. Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l1\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l1\_metric\_1 : \iota \Rightarrow o$  be given. Let  $m1\_topmetr : \iota \Rightarrow \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned}
 & \forall X0.(v1\_xreal\_0 X0) \Rightarrow (\forall X1.(v1\_xreal\_0 X1) \Rightarrow (\forall X2. \\
 & ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 k5\_numbers (u1\_struct\_0 (k2\_topmetr \\
 & X0 X1))) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers \\
 & (u1\_struct\_0 (k2\_topmetr X0 X1)))))) \Rightarrow (\forall X3.((v1\_funct\_1 \\
 & X3) \wedge ((v1\_funct\_2 X3 k5\_numbers (u1\_struct\_0 k8\_metric\_1)) \wedge ( \\
 & m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (u1\_struct\_0 \\
 & k8\_metric\_1)))))) \Rightarrow (((r1\_funct\_2 k5\_numbers (u1\_struct\_0 k8\_metric\_1) \\
 & k5\_numbers (u1\_struct\_0 (k2\_topmetr X0 X1)) X3 X2) \wedge (r1\_xxreal\_0 \\
 & X0 X1)) \Rightarrow (((v2\_tbsp\_1 X3 k8\_metric\_1) \Rightarrow (v2\_tbsp\_1 X2 (k2\_topmetr \\
 & X0 X1))) \wedge (((v2\_tbsp\_1 X2 (k2\_topmetr X0 X1)) \Rightarrow (v2\_tbsp\_1 X3 k8\_metric\_1)) \wedge \\
 & ((v2\_tbsp\_1 X3 k8\_metric\_1) \Rightarrow (k1\_tbsp\_1 k8\_metric\_1 X3 = k1\_tbsp\_1 \\
 & (k2\_topmetr X0 X1) X2)))))))))
 \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(v1\_xreal\_0 X0) \Rightarrow (\forall X1.(v1\_xreal\_0 X1) \Rightarrow (\forall X2. \\
& ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 k5\_numbers (u1\_struct\_0 (k2\_topmetr \\
& X0 X1))) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers \\
& (u1\_struct\_0 (k2\_topmetr X0 X1))))))) \Rightarrow ((r1\_xreal\_0 X0 X1) \Rightarrow ( \\
& (v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 k5\_numbers (u1\_struct\_0 k8\_metric\_1)) \wedge \\
& (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (u1\_struct\_0 \\
& k8\_metric\_1))))))))))
\end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_funct\_1 X0) \wedge ((v1\_funct\_2 X0 k5\_numbers k1\_numbers) \wedge \\
& (m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))) \Rightarrow \\
& (\forall X1.((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 X1 k5\_numbers (u1\_struct\_0 \\
& k8\_metric\_1)) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers \\
& (u1\_struct\_0 k8\_metric\_1)))))) \Rightarrow ((r1\_funct\_2 k5\_numbers k1\_numbers \\
& k5\_numbers (u1\_struct\_0 k8\_metric\_1) X0 X1) \Rightarrow (((v2\_comseq\_2 X0) \Rightarrow \\
& (v2\_tbsp\_1 X1 k8\_metric\_1)) \wedge (((v2\_tbsp\_1 X1 k8\_metric\_1) \Rightarrow (v2\_comseq\_2 \\
& X0)) \wedge ((v2\_comseq\_2 X0) \Rightarrow (k2\_seq\_2 X0 = k1\_tbsp\_1 k8\_metric\_1 X1))))))
\end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.\forall X2.\forall X3.\forall X4.\forall X5. \\
& ((\neg v1\_xboole\_0 X1) \wedge ((\neg v1\_xboole\_0 X3) \wedge (((v1\_funct\_1 X4) \wedge (( \\
& v1\_funct\_2 X4 X0 X1) \wedge (m1\_subset\_1 X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& X0 X1)))))) \wedge ((v1\_funct\_1 X5) \wedge ((v1\_funct\_2 X5 X2 X3) \wedge (m1\_subset\_1 \\
& X5 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X2 X3))))))) \Rightarrow ((r1\_funct\_2 X0 X1 \\
& X2 X3 X4 X5) \Leftrightarrow (X4 = X5))
\end{aligned} \tag{4}$$

Assume the following.

$$(v1\_metric\_1 k8\_metric\_1) \wedge ((v6\_metric\_1 k8\_metric\_1) \wedge ((v7\_metric\_1 \\
k8\_metric\_1) \wedge ((v8\_metric\_1 k8\_metric\_1) \wedge (v9\_metric\_1 k8\_metric\_1)))) \tag{5}$$

Assume the following.

$$(\neg v2\_struct\_0 k8\_metric\_1) \wedge (v1\_metric\_1 k8\_metric\_1) \tag{6}$$

Assume the following.

$$\forall X0.((\neg v2\_struct\_0 X0) \wedge (l1\_struct\_0 X0)) \Rightarrow (\neg v1\_xboole\_0 \\
(u1\_struct\_0 X0)) \tag{7}$$

Assume the following.

$$\neg v1\_xboole\_0 k1\_numbers \tag{8}$$

Assume the following.

$$\begin{aligned} \forall X0.((v6\_metric\_1 X0) \wedge ((v7\_metric\_1 X0) \wedge ((v8\_metric\_1 \\ X0) \wedge ((v9\_metric\_1 X0) \wedge (l1\_metric\_1 X0)))))) \Rightarrow (\forall X1.(m1\_topmetr \\ X1 X0) \Rightarrow ((v6\_metric\_1 X1) \wedge ((v7\_metric\_1 X1) \wedge ((v8\_metric\_1 X1) \wedge \\ ((v9\_metric\_1 X1) \wedge (l1\_metric\_1 X1)))))) \end{aligned} \quad (9)$$

Assume the following.

$$\forall X0.(l1\_metric\_1 X0) \Rightarrow (l1\_struct\_0 X0) \quad (10)$$

Assume the following.

$$(v1\_metric\_1 k8\_metric\_1) \wedge (l1\_metric\_1 k8\_metric\_1) \quad (11)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((v1\_xreal\_0 X0) \wedge (v1\_xreal\_0 X1)) \Rightarrow ((\neg \\ v2\_struct\_0 (k2\_topmetr X0 X1)) \wedge ((v1\_metric\_1 (k2\_topmetr X0 \\ X1)) \wedge (m1\_topmetr (k2\_topmetr X0 X1) k8\_metric\_1))) \end{aligned} \quad (12)$$

**Theorem 1**

$$\begin{aligned} \forall X0.(v1\_xreal\_0 X0) \Rightarrow (\forall X1.(v1\_xreal\_0 X1) \Rightarrow (\forall X2. \\ ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 k5\_numbers k1\_numbers) \wedge (m1\_subset\_1 \\ X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \Rightarrow (\forall X3. \\ ((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 k5\_numbers (u1\_struct\_0 (k2\_topmetr \\ X0 X1))) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers \\ (u1\_struct\_0 (k2\_topmetr X0 X1)))))))) \Rightarrow (((r1\_funct\_2 k5\_numbers \\ (u1\_struct\_0 (k2\_topmetr X0 X1)) k5\_numbers k1\_numbers X3 X2) \wedge \\ ((r1\_xreal\_0 X0 X1) \wedge (v2\_comseq\_2 X2))) \Rightarrow ((v2\_tbsp\_1 X3 (k2\_topmetr \\ X0 X1)) \wedge (k2\_seq\_2 X2 = k1\_tbsp\_1 (k2\_topmetr X0 X1) X3)))))) \end{aligned}$$