

t93_rfunct_1
(TMUz8chRz2iqS9R6PxqbgY6QnmuGjKcr4xv)

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Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_numbers : \iota$ be given. Let $v1_seq_2 : \iota \Rightarrow o$ be given. Let $k2_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v3_funct_1 : \iota \Rightarrow o$ be given. Let $k3_valued_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k3_xboole_0 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v2_seq_2 : \iota \Rightarrow o$ be given. Let $v1_comseq_2 : \iota \Rightarrow o$ be given. Let $v1_relat_1 : \iota \Rightarrow o$ be given. Let $v3_valued_0 : \iota \Rightarrow o$ be given. Let $k5_relat_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_valued_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v3_membered : \iota \Rightarrow o$ be given. Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. ((v1_relat_1 X2) \wedge ((v1_funct_1 \\ & \quad X2) \wedge (v3_valued_0 X2))) \Rightarrow (\forall X3. ((v1_relat_1 X3) \wedge ((v1_funct_1 \\ & \quad X3) \wedge (v3_valued_0 X3))) \Rightarrow (((v1_seq_2 (k5_relat_1 X2 X0)) \wedge (v1_seq_2 \\ & \quad (k5_relat_1 X3 X1))) \Rightarrow (v1_seq_2 (k5_relat_1 (k1_valued_1 X2 X3) \\ & \quad (k3_xboole_0 X0 X1)))) \wedge (((v2_seq_2 (k5_relat_1 X2 X0)) \wedge (v2_seq_2 \\ & \quad (k5_relat_1 X3 X1))) \Rightarrow (v2_seq_2 (k5_relat_1 (k1_valued_1 X2 X3) \\ & \quad (k3_xboole_0 X0 X1)))) \wedge (((v1_comseq_2 (k5_relat_1 X2 X0)) \wedge (v1_comseq_2 \\ & \quad (k5_relat_1 X3 X1))) \Rightarrow (v1_comseq_2 (k5_relat_1 (k1_valued_1 X2 \\ & \quad X3) (k3_xboole_0 X0 X1)))))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. \forall X4. ((v3_membered \\ & \quad X1) \wedge ((v3_membered X2) \wedge (((v1_funct_1 X3) \wedge (m1_subset_1 X3 (k1_zfmisc_1 \\ & \quad (k2_zfmisc_1 X0 X1)))) \wedge ((v1_funct_1 X4) \wedge (m1_subset_1 X4 (k1_zfmisc_1 \\ & \quad (k2_zfmisc_1 X0 X2)))))) \Rightarrow (k3_valued_1 X0 X1 X2 X3 X4 = k1_valued_1 \\ & \quad X3 X4) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. ((v1_funct_1 X2) \wedge \\ & \quad (m1_subset_1 X2 (k1_zfmisc_1 (k2_zfmisc_1 X0 X1)))) \Rightarrow (k2_partfun1 \\ & \quad X0 X1 X2 X3 = k5_relat_1 X2 X3) \end{aligned} \tag{3}$$

Assume the following.

$$\forall X0.\forall X1.((v1_relat_1 X0)\wedge(v3_valued_0 X0))\Rightarrow((v1_relat_1 (k5_relat_1 X0 X1))\wedge(v3_valued_0 (k5_relat_1 X0 X1))) \quad (4)$$

Assume the following.

$$v3_membered k1_numbers \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.\forall X4.((v3_membered \\ & X1)\wedge((v3_membered X2)\wedge(((v1_funct_1 X3)\wedge(m1_subset_1 X3 (k1_zfmisc_1 \\ & (k2_zfmisc_1 X0 X1))))\wedge((v1_funct_1 X4)\wedge(m1_subset_1 X4 (k1_zfmisc_1 \\ & (k2_zfmisc_1 X0 X2))))))\Rightarrow((v1_funct_1 (k3_valued_1 X0 X1 X2 X3 \\ & X4))\wedge(m1_subset_1 (k3_valued_1 X0 X1 X2 X3 X4) (k1_zfmisc_1 (k2_zfmisc_1 \\ & X0 k1_numbers)))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.((v1_funct_1 X2)\wedge \\ & (m1_subset_1 X2 (k1_zfmisc_1 (k2_zfmisc_1 X0 X1))))\Rightarrow((v1_funct_1 \\ & (k2_partfun1 X0 X1 X2 X3))\wedge(m1_subset_1 (k2_partfun1 X0 X1 X2 X3) \\ & (k1_zfmisc_1 (k2_zfmisc_1 X0 X1)))) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1_relat_1 X0)\wedge((v1_funct_1 X0)\wedge((v3_valued_0 \\ & X0)\wedge(v1_comseq_2 X0))))\Rightarrow((v1_relat_1 X0)\wedge((v1_funct_1 X0)\wedge \\ & ((v3_valued_0 X0)\wedge((v1_seq_2 X0)\wedge(v2_seq_2 X0)))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1_relat_1 X0)\wedge((v1_funct_1 X0)\wedge((v3_funct_1 X0)\wedge \\ & (v3_valued_0 X0))))\Rightarrow((v1_relat_1 X0)\wedge((v1_funct_1 X0)\wedge((v3_valued_0 \\ & X0)\wedge(v1_comseq_2 X0)))) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(m1_subset_1 X2 (k1_zfmisc_1 \\ & (k2_zfmisc_1 X0 X1)))\Rightarrow(v1_relat_1 X2) \end{aligned} \quad (10)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(v3_membered X1)\Rightarrow(\forall X2.(m1_subset_1 \\ & X2 (k1_zfmisc_1 (k2_zfmisc_1 X0 X1)))\Rightarrow(v3_valued_0 X2)) \end{aligned} \quad (11)$$

Theorem 1

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (\neg v1_xboole_0 X2) \Rightarrow (\forall X3. \\ & ((v1_funct_1 X3) \wedge (m1_subset_1 X3 (k1_zfmisc_1 (k2_zfmisc_1 X2 \\ & k1_numbers)))) \Rightarrow (\forall X4. ((v1_funct_1 X4) \wedge (m1_subset_1 X4 \\ & (k1_zfmisc_1 (k2_zfmisc_1 X2 k1_numbers)))) \Rightarrow (((v1_seq_2 (k2_partfun1 \\ & X2 k1_numbers X3 X0)) \wedge (v3_funct_1 (k2_partfun1 X2 k1_numbers X4 \\ & X1))) \Rightarrow (v1_seq_2 (k2_partfun1 X2 k1_numbers (k3_valued_1 X2 k1_numbers \\ & k1_numbers X3 X4) (k3_xboole_0 X0 X1)))) \wedge (((v2_seq_2 (k2_partfun1 \\ & X2 k1_numbers X3 X0)) \wedge (v3_funct_1 (k2_partfun1 X2 k1_numbers X4 \\ & X1))) \Rightarrow (v2_seq_2 (k2_partfun1 X2 k1_numbers (k3_valued_1 X2 k1_numbers \\ & k1_numbers X3 X4) (k3_xboole_0 X0 X1)))) \wedge (((v1_comseq_2 (k2_partfun1 \\ & X2 k1_numbers X3 X0)) \wedge (v3_funct_1 (k2_partfun1 X2 k1_numbers X4 \\ & X1))) \Rightarrow (v1_comseq_2 (k2_partfun1 X2 k1_numbers (k3_valued_1 X2 \\ & k1_numbers k1_numbers X3 X4) (k3_xboole_0 X0 X1))))))))) \end{aligned}$$