

# t94\_semi\_af1 (TMTLUvsgsnUHQNEsikPx- CvAhkMnYzKkEzU6)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v1\_semi\_af1 : \iota \Rightarrow o$  be given. Let  $l1\_analoaf : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $r4\_semi\_af1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r2\_analoaf : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_semi\_af1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v1\_semi\_af1 X0) \wedge (l1\_analoaf \\
& \quad X0))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2. \\
& \quad (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 \\
& \quad (u1\_struct\_0 X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow \\
& \quad ((r2\_analoaf X0 X1 X2 X3 X4) \Rightarrow ((r2\_analoaf X0 X2 X1 X3 X4) \wedge ((r2\_analoaf \\
& \quad X0 X1 X2 X4 X3) \wedge ((r2\_analoaf X0 X2 X1 X4 X3) \wedge ((r2\_analoaf X0 X3 X4 X1 \\
& \quad X2) \wedge ((r2\_analoaf X0 X4 X3 X1 X2) \wedge ((r2\_analoaf X0 X3 X4 X2 X1) \wedge (r2\_analoaf \\
& \quad X0 X4 X3 X2 X1))))))))))
\end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v1\_semi\_af1 X0) \wedge (l1\_analoaf \\
& \quad X0))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2. \\
& \quad (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 \\
& \quad (u1\_struct\_0 X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow \\
& \quad (\forall X5.(m1\_subset\_1 X5 (u1\_struct\_0 X0)) \Rightarrow ((r4\_semi\_af1 \\
& \quad X0 X1 X2 X3 X4 X5) \Leftrightarrow ((\neg r1\_semi\_af1 X0 X5 X1 X3) \wedge ((r1\_semi\_af1 X0 X5 \\
& \quad X1 X2) \wedge ((r1\_semi\_af1 X0 X5 X3 X4) \wedge (r2\_analoaf X0 X1 X3 X2 X4))))))))))
\end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v1\_semi\_af1 X0) \wedge (l1\_analoaf \\
& \quad X0))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2. \\
& \quad (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 \\
& \quad (u1\_struct\_0 X0)) \Rightarrow ((r1\_semi\_af1 X0 X1 X2 X3) \Leftrightarrow (r2\_analoaf X0 X1 \\
& \quad X2 X1 X3))))))
\end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge (l1\_analoaf X0)) \Rightarrow ((v1\_semi\_af1 \\
& X0) \Leftrightarrow ((\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2. \\
& (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (r2\_analoaf X0 X1 X2 X2 X1)))) \wedge \\
& ((\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.( \\
& m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 \\
& (u1\_struct\_0 X0)) \Rightarrow (r2\_analoaf X0 X1 X2 X3 X3)))) \wedge ((\forall X1. \\
& (m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 \\
& (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 X0)) \Rightarrow \\
& (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow (\forall X5.(m1\_subset\_1 \\
& X5 (u1\_struct\_0 X0)) \Rightarrow (\forall X6.(m1\_subset\_1 X6 (u1\_struct\_0 \\
& X0)) \Rightarrow (((r2\_analoaf X0 X1 X2 X3 X4) \wedge (r2\_analoaf X0 X1 X2 X5 X6)) \Rightarrow ( \\
& (X1 = X2) \vee (r2\_analoaf X0 X3 X4 X5 X6)))))) \wedge ((\forall X1.(m1\_subset\_1 \\
& X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 \\
& X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 X0)) \Rightarrow ((r2\_analoaf \\
& X0 X1 X2 X1 X3) \Rightarrow (r2\_analoaf X0 X2 X1 X2 X3)))) \wedge ((\neg \forall X1.(m1\_subset\_1 \\
& X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 \\
& X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 X0)) \Rightarrow (r2\_analoaf \\
& X0 X1 X2 X1 X3)))) \wedge ((\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow \\
& (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 \\
& X3 (u1\_struct\_0 X0)) \Rightarrow (\exists X4.(m1\_subset\_1 X4 (u1\_struct\_0 \\
& X0)) \wedge ((r2\_analoaf X0 X1 X2 X3 X4) \wedge (r2\_analoaf X0 X1 X3 X2 X4)))))) \wedge \\
& ((\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.( \\
& m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\exists X3.(m1\_subset\_1 X3 \\
& (u1\_struct\_0 X0)) \wedge (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow \\
& (\forall X5.(m1\_subset\_1 X5 (u1\_struct\_0 X0)) \Rightarrow ((r2\_analoaf X0 \\
& X1 X2 X1 X3) \wedge (\neg \forall X6.(m1\_subset\_1 X6 (u1\_struct\_0 X0)) \Rightarrow (( \\
& r2\_analoaf X0 X1 X3 X1 X4) \wedge (\neg (r2\_analoaf X0 X1 X5 X1 X6) \wedge (r2\_analoaf \\
& X0 X3 X5 X4 X6)))))) \wedge ((\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 \\
& X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3. \\
& (m1\_subset\_1 X3 (u1\_struct\_0 X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 \\
& (u1\_struct\_0 X0)) \Rightarrow (\forall X5.(m1\_subset\_1 X5 (u1\_struct\_0 X0)) \Rightarrow \\
& (\forall X6.(m1\_subset\_1 X6 (u1\_struct\_0 X0)) \Rightarrow (\forall X7.(m1\_subset\_1 \\
& X7 (u1\_struct\_0 X0)) \Rightarrow (((r2\_analoaf X0 X1 X2 X1 X3) \wedge ((r2\_analoaf \\
& X0 X1 X4 X1 X5) \wedge ((r2\_analoaf X0 X1 X6 X1 X7) \wedge ((r2\_analoaf X0 X2 X4 X3 \\
& X5) \wedge (r2\_analoaf X0 X2 X6 X3 X7)))))) \Rightarrow ((r2\_analoaf X0 X1 X2 X1 X4) \vee \\
& ((r2\_analoaf X0 X1 X2 X1 X6) \vee (r2\_analoaf X0 X4 X6 X5 X7)))))) \wedge \\
& ((\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.( \\
& m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 \\
& (u1\_struct\_0 X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow \\
& (\forall X5.(m1\_subset\_1 X5 (u1\_struct\_0 X0)) \Rightarrow (\forall X6.(m1\_subset\_1 \\
& X6 (u1\_struct\_0 X0)) \Rightarrow (((r2\_analoaf X0 X1 X2 X3 X4) \wedge ((r2\_analoaf \\
& X0 X1 X2 X5 X6) \wedge ((r2\_analoaf X0 X1 X3 X2 X4) \wedge (r2\_analoaf X0 X1 X5 X2 \\
& X6)))) \Rightarrow ((r2\_analoaf X0 X1 X2 X1 X3) \vee ((r2\_analoaf X0 X1 X2 X1 X5) \vee \\
& (r2\_analoaf X0 X3 X5 X4 X6)))))) \wedge ((\forall X1.(m1\_subset\_1 \\
& X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 \\
& X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 X0)) \Rightarrow (\forall X4. \\
& (m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow (\forall X5.(m1\_subset\_1 X5 \\
& (u1\_struct\_0 X0)) \Rightarrow (\forall X6.(m1\_subset\_1 X6 (u1\_struct\_0 X0)) \Rightarrow \\
& (((r2\_analoaf X0 X1 X2 X1 X3) \wedge ((r2\_analoaf X0 X4 X5 X4 X6) \wedge ((r2\_analoaf \\
& X0 X1 X5 X2 X4) \wedge (r2\_analoaf X0 X2 X6 X3 X5)))) \Rightarrow (r2\_analoaf X0 X3 X4 \\
& X1 X6)))))) \wedge ((\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow \\
& (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 \\
& X3 (u1\_struct\_0 X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 \\
& X0)) \Rightarrow (\neg (\neg r2\_analoaf X0 X1 X2 X1 X3) \wedge ((r2\_analoaf X0 X1 X2 X3 X4) \wedge \\
& ((r2\_analoaf X0 X1 X3 X2 X4) \wedge (r2\_analoaf X0 X1 X4 X2 X3)))))) \wedge (((4))
\end{aligned}$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v1\_semi\_af1 X0) \wedge (l1\_analoaf \\ & X0))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2. \\ & (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 \\ & (u1\_struct\_0 X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow \\ & ((r4\_semi\_af1 X0 X1 X2 X3 X4 X4) \Rightarrow (X4 = X2)))))) \end{aligned}$$