# t96_member_1 <br> (TMQLm7KEeH6eDYgb2PQ8jrnxAtnSaSekxHf) 

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Let $v 1 \_$membered $: \iota \Rightarrow 0$ be given. Let $r$ 1_tarski : $\iota \Rightarrow \iota \Rightarrow 0$ be given. Let $k 13 \_m e m b e r \_1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k$ 11_member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let k9_member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let k5_member_1: $\iota \Rightarrow \iota$ be given. Assume the following.

$$
\forall X 0 .\left(v 1 \_ \text {membered } X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_ \text {membered } X 1\right) \Rightarrow(\forall X 2 \text {. }\right.
$$

(v1_membered $X 2) \Rightarrow\left(r 1 \_t a r s k i\left(k 13 \_m e m b e r \_1 ~ X 0 ~\left(k 9 \_m e m b e r \_1 ~ X 1 ~\right.\right.\right.$
X2)) (k9_member_1 (k13_member_1 X0 X1) (k13_member_1 X0 X2)) ))
Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow\left(k 13 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0\left(k 5 \_m e m b e r \_1 X 1\right)=k 5 \_m e m b e r \_1\left(k 13 \_m e m b e r \_1 X 0 X 1\right)\right)\right) \tag{2}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 1 \_m e m b e r e d \quad X 0\right) \wedge\left(v 1 \_m e m b e r e d ~ X 1\right)\right) \Rightarrow( \\
\left.v 1 \_m e m b e r e d ~\left(k 13 \_m e m b e r \_1 X 0 X 1\right)\right) \tag{3}
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d\left(k 5 \_m e m b e r \_1 X 0\right)\right) \tag{4}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow\left(k 11 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 9 \_m e m b e r \_1 X 0\left(k 5 \_m e m b e r \_1 X 1\right)\right)\right) \tag{5}
\end{gather*}
$$

## Theorem 1

$\forall X 0 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d \quad X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 1 \_m e m b e r e d X 2\right) \Rightarrow\left(r 1 \_\right.$tarski $\left(k 13 \_m e m b e r \_1 X 0\left(k 11 \_m e m b e r \_1 X 1\right.\right.$
$\left.\left.X 2))\left(k 11 \_m e m b e r \_1\left(k 13 \_m e m b e r \_1 X 0 X 1\right)\left(k 13 \_m e m b e r \_1 X 0 X 2\right)\right)\right)\right)$

