

t9\_extpro\_1  
(TMS6Xdtx4KtDoMqLKkniFaqCcLdVNgNTCoh)

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_setfam\_1 : \iota \Rightarrow o$  be given. Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_memstr\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v3\_memstr\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l1\_extpro\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_numbers : \iota$  be given. Let  $k5\_numbers : \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_compos\_1 : \iota \Rightarrow \iota$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v5\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $r1\_tarski : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k16\_funcop\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $v5\_funct\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_memstr\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k4\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k3\_extpro\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k9\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $k2\_funcop\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k10\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_tarski : \iota \Rightarrow \iota$  be given. Let  $k7\_funcop\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $l1\_memstr\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l1\_compos\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_memstr\_0 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k7\_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0. \forall X1. k1\_funct\_1 (k16\_funcop\_1 X0 X1) X0 = X1 \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. \neg (X0 \in X1) \wedge ((m1\_subset\_1 X1 (k1\_zfmisc\_1 X2)) \wedge (v1\_xboole\_0 X2)) \quad (2)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. ((X0 \in X1) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 X2))) \Rightarrow (m1\_subset\_1 X0 X2) \quad (3)$$

Assume the following.

$$\forall X0. \forall X1. (m1\_subset\_1 X0 (k1\_zfmisc\_1 X1)) \Leftrightarrow (r1\_tarski X0 X1) \quad (4)$$

Assume the following.

$$\forall X0.\forall X1.(m1\_subset\_1 X0 X1)\Rightarrow((v1\_xboole\_0 X1)\vee (X0 \in X1)) \quad (5)$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_relat\_1 X0)\wedge(v1\_funct\_1 X0))\Rightarrow(\forall X1.(( \\ v1\_relat\_1 X1)\wedge(v1\_funct\_1 X1))\Rightarrow((r1\_tarski X0 X1)\Leftrightarrow((r1\_tarski \\ (k9\_xtuple\_0 X0) (k9\_xtuple\_0 X1))\wedge(\forall X2.(X2 \in k9\_xtuple\_0 \\ X0)\Rightarrow(k1\_funct\_1 X0 X2 = k1\_funct\_1 X1 X2)))))) \end{aligned} \quad (6)$$

Assume the following.

$$\forall X0.\forall X1.(k9\_xtuple\_0 (k2\_funcop\_1 X0 X1) = X0)\wedge( r1\_tarski (k10\_xtuple\_0 (k2\_funcop\_1 X0 X1)) (k1\_tarski X1)) \quad (7)$$

Assume the following.

$$\begin{aligned} \forall X0.(v1\_relat\_1 X0)\Rightarrow(\forall X1.(v1\_relat\_1 X1)\Rightarrow((r1\_tarski \\ X0 X1)\Rightarrow((r1\_tarski (k9\_xtuple\_0 X0) (k9\_xtuple\_0 X1))\wedge(r1\_tarski \\ (k10\_xtuple\_0 X0) (k10\_xtuple\_0 X1)))))) \end{aligned} \quad (8)$$

Assume the following.

$$\forall X0.\forall X1.k7\_funcop\_1 X0 X1 = k2\_funcop\_1 X0 X1 \quad (9)$$

Assume the following.

$$\forall X0.\forall X1.(l1\_extpro\_1 X1 X0)\Rightarrow((l1\_memstr\_0 X1 X0)\wedge (l1\_compos\_1 X1)) \quad (10)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.(v1\_funct\_1 (k7\_funcop\_1 X0 X1))\wedge((v1\_funct\_2 \\ (k7\_funcop\_1 X0 X1) X0 (k1\_tarski X1))\wedge(m1\_subset\_1 (k7\_funcop\_1 \\ X0 X1) (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 (k1\_tarski X1)))))) \end{aligned} \quad (11)$$

Assume the following.

$$\forall X0.\forall X1.k16\_funcop\_1 X0 X1 = k7\_funcop\_1 (k1\_tarski X0) X1 \quad (12)$$

Assume the following.

$$\begin{aligned} \forall X0.(\neg v1\_setfam\_1 X0)\Rightarrow(\forall X1.((\neg v2\_struct\_0 X1)\wedge \\ ((v2\_memstr\_0 X1 X0)\wedge((v3\_memstr\_0 X1 X0)\wedge(l1\_memstr\_0 X1 X0))))\Rightarrow \\ (\forall X2.((v1\_relat\_1 X2)\wedge((v4\_relat\_1 X2 (u1\_struct\_0 X1))\wedge \\ ((v1\_funct\_1 X2)\wedge(v5\_funct\_1 X2 (k2\_memstr\_0 X0 X1))))))\Rightarrow(k5\_memstr\_0 \\ X0 X1 X2 = k1\_funct\_1 X2 (k4\_struct\_0 X1)))) \end{aligned} \quad (13)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_relat\_1 X1)\wedge((v5\_relat\_1 X1 X0)\wedge(v1\_funct\_1 X1)))\Rightarrow(\forall X2.(X2 \in k9\_xtuple\_0 X1)\Rightarrow(k7\_partfun1 X0 X1 X2 = k1\_funct\_1 X1 X2)) \quad (14)$$

Assume the following.

$$\begin{aligned} & \forall X0.(\neg v1\_setfam\_1 X0)\Rightarrow(\forall X1.((\neg v2\_struct\_0 X1)\wedge \\ & ((v2\_memstr\_0 X1 X0)\wedge((v3\_memstr\_0 X1 X0)\wedge(l1\_extpro\_1 X1 X0))))\Rightarrow \\ & (\forall X2.((v1\_relat\_1 X2)\wedge((v5\_relat\_1 X2 (u1\_compos\_1 X1))\wedge \\ & (v1\_funct\_1 X2)))\Rightarrow(\forall X3.((v1\_relat\_1 X3)\wedge((v4\_relat\_1 \\ & X3 (u1\_struct\_0 X1))\wedge((v1\_funct\_1 X3)\wedge((v5\_funct\_1 X3 (k2\_memstr\_0 \\ & X0 X1))\wedge(v1\_partfun1 X3 (u1\_struct\_0 X1))))))\Rightarrow(k3\_extpro\_1 X0 \\ & X1 X2 X3 = k7\_partfun1 (u1\_compos\_1 X1) X2 (k5\_memstr\_0 X0 X1 X3)))))) \quad (15) \end{aligned}$$

Assume the following.

$$\forall X0.\forall X1.k2\_funcop\_1 X0 X1 = k2\_zfmisc\_1 X0 (k1\_tarski X1) \quad (16)$$

Assume the following.

$$\forall X0.\forall X1.(X1 = k1\_tarski X0)\Leftrightarrow(\forall X2.(X2 \in X1)\Leftrightarrow(X2 = X0)) \quad (17)$$

Assume the following.

$$\forall X0.(v1\_relat\_1 X0)\Rightarrow(\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 X0))\Rightarrow(v1\_relat\_1 X1)) \quad (18)$$

### Theorem 1

$$\begin{aligned} & \forall X0.((\neg v1\_xboole\_0 X0)\wedge(\neg v1\_setfam\_1 X0))\Rightarrow(\forall X1. \\ & ((\neg v2\_struct\_0 X1)\wedge((v2\_memstr\_0 X1 X0)\wedge((v3\_memstr\_0 X1 X0)\wedge \\ & (l1\_extpro\_1 X1 X0))))\Rightarrow(\forall X2.(m2\_subset\_1 X2 k1\_numbers \\ & k5\_numbers)\Rightarrow(\forall X3.(m1\_subset\_1 X3 (u1\_compos\_1 X1))\Rightarrow( \\ & \forall X4.((v1\_relat\_1 X4)\wedge((v4\_relat\_1 X4 k5\_numbers)\wedge((v5\_relat\_1 \\ & X4 (u1\_compos\_1 X1))\wedge(v1\_funct\_1 X4))))\Rightarrow((r1\_tarski (k16\_funcop\_1 \\ & X2 X3) X4)\Rightarrow(\forall X5.((v1\_relat\_1 X5)\wedge((v4\_relat\_1 X5 (u1\_struct\_0 \\ & X1))\wedge((v1\_funct\_1 X5)\wedge((v5\_funct\_1 X5 (k2\_memstr\_0 X0 X1))\wedge( \\ & v1\_partfun1 X5 (u1\_struct\_0 X1))))))\Rightarrow((r1\_tarski (k16\_funcop\_1 \\ & (k4\_struct\_0 X1) X2) X5)\Rightarrow(k3\_extpro\_1 X0 X1 X4 X5 = X3))))))))) \end{aligned}$$