

## t9\_topalg\_1

(TMS7onLZXgddXmaEzrJAtDwaybzRgaFG8Dt)

October 27, 2020

Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_finseq\_1 : \iota \Rightarrow o$  be given. Let  $v3\_valued\_0 : \iota \Rightarrow o$  be given. Let  $k8\_rvsum\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_rvsum\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k45\_valued\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_valued\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_valued\_0 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge ((v3\_valued\_0 \\ & X0) \wedge (v1\_finseq\_1 X0)))) \Rightarrow (\forall X1.((v1\_relat\_1 X1) \wedge ((v1\_funct\_1 \\ & X1) \wedge ((v3\_valued\_0 X1) \wedge (v1\_finseq\_1 X1)))) \Rightarrow (\forall X2.((v1\_relat\_1 \\ & X2) \wedge ((v1\_funct\_1 X2) \wedge ((v3\_valued\_0 X2) \wedge (v1\_finseq\_1 X2)))) \Rightarrow \\ & (k4\_rvsum\_1 X0 (k8\_rvsum\_1 X1 X2) = k8\_rvsum\_1 (k4\_rvsum\_1 X0 X1 \\ & X2))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge ((v3\_valued\_0 \\ & X0) \wedge (v1\_finseq\_1 X0)))) \Rightarrow (\forall X1.((v1\_relat\_1 X1) \wedge ((v1\_funct\_1 \\ & X1) \wedge ((v3\_valued\_0 X1) \wedge (v1\_finseq\_1 X1)))) \Rightarrow (\forall X2.((v1\_relat\_1 \\ & X2) \wedge ((v1\_funct\_1 X2) \wedge ((v3\_valued\_0 X2) \wedge (v1\_finseq\_1 X2)))) \Rightarrow \\ & (k8\_rvsum\_1 (k8\_rvsum\_1 X0 X1) X2 = k8\_rvsum\_1 X0 (k4\_rvsum\_1 X1 \\ & X2))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. (((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (( \\ & v3\_valued\_0 X0) \wedge (v1\_finseq\_1 X0)))) \wedge ((v1\_relat\_1 X1) \wedge ((v1\_funct\_1 \\ & X1) \wedge ((v3\_valued\_0 X1) \wedge (v1\_finseq\_1 X1)))))) \Rightarrow (k8\_rvsum\_1 X0 X1 = \\ & k45\_valued\_1 X0 X1) \end{aligned} \tag{3}$$

Assume the following.

$$\forall X0.\forall X1.(((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge((v3\_valued\_0 X0)\wedge(v1\_finseq\_1 X0))))\wedge((v1\_relat\_1 X1)\wedge((v1\_funct\_1 X1)\wedge((v3\_valued\_0 X1)\wedge(v1\_finseq\_1 X1))))))\Rightarrow(k4\_rvsum\_1 X0 X1 = k1\_valued\_1 X0 X1) \quad (4)$$

Assume the following.

$$\forall X0.\forall X1.(((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge((v1\_valued\_0 X0)\wedge(v1\_finseq\_1 X0))))\wedge((v1\_relat\_1 X1)\wedge((v1\_funct\_1 X1)\wedge((v1\_valued\_0 X1)\wedge(v1\_finseq\_1 X1))))))\Rightarrow((v1\_relat\_1 (k45\_valued\_1 X0 X1))\wedge((v1\_funct\_1 (k45\_valued\_1 X0 X1))\wedge(v1\_finseq\_1 (k45\_valued\_1 X0 X1)))) \quad (5)$$

Assume the following.

$$\forall X0.\forall X1.(((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge(v3\_valued\_0 X0)))\wedge((v1\_relat\_1 X1)\wedge((v1\_funct\_1 X1)\wedge(v3\_valued\_0 X1))))\Rightarrow((v1\_relat\_1 (k45\_valued\_1 X0 X1))\wedge((v1\_funct\_1 (k45\_valued\_1 X0 X1))\wedge(v3\_valued\_0 (k45\_valued\_1 X0 X1)))) \quad (6)$$

Assume the following.

$$\forall X0.\forall X1.(((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge(v3\_valued\_0 X0)))\wedge((v1\_relat\_1 X1)\wedge((v1\_funct\_1 X1)\wedge(v3\_valued\_0 X1))))\Rightarrow((v1\_relat\_1 (k1\_valued\_1 X0 X1))\wedge((v1\_funct\_1 (k1\_valued\_1 X0 X1))\wedge(v3\_valued\_0 (k1\_valued\_1 X0 X1)))) \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.(((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge((v1\_valued\_0 X0)\wedge(v1\_finseq\_1 X0))))\wedge((v1\_relat\_1 X1)\wedge((v1\_funct\_1 X1)\wedge((v1\_valued\_0 X1)\wedge(v1\_finseq\_1 X1))))))\Rightarrow((v1\_relat\_1 (k1\_valued\_1 X0 X1))\wedge((v1\_funct\_1 (k1\_valued\_1 X0 X1))\wedge(v1\_finseq\_1 (k1\_valued\_1 X0 X1)))) \quad (8)$$

Assume the following.

$$\forall X0.\forall X1.(((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge((v3\_valued\_0 X0)\wedge(v1\_finseq\_1 X0))))\wedge((v1\_relat\_1 X1)\wedge((v1\_funct\_1 X1)\wedge((v3\_valued\_0 X1)\wedge(v1\_finseq\_1 X1))))))\Rightarrow(k4\_rvsum\_1 X0 X1 = k4\_rvsum\_1 X1 X0) \quad (9)$$

Assume the following.

$$\forall X0.((v1\_relat\_1 X0)\wedge(v3\_valued\_0 X0))\Rightarrow((v1\_relat\_1 X0)\wedge(v1\_valued\_0 X0)) \quad (10)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge ((v1\_finseq\_1 \\ & X0) \wedge (v3\_valued\_0 X0)))) \Rightarrow (\forall X1.((v1\_relat\_1 X1) \wedge ((v1\_funct\_1 \\ & X1) \wedge ((v1\_finseq\_1 X1) \wedge (v3\_valued\_0 X1)))) \Rightarrow (\forall X2.((v1\_relat\_1 \\ & X2) \wedge ((v1\_funct\_1 X2) \wedge ((v1\_finseq\_1 X2) \wedge (v3\_valued\_0 X2)))) \Rightarrow \\ & (\forall X3.((v1\_relat\_1 X3) \wedge ((v1\_funct\_1 X3) \wedge ((v1\_finseq\_1 \\ & X3) \wedge (v3\_valued\_0 X3)))) \Rightarrow (k8\_rvsum\_1 (k4\_rvsum\_1 X0 X1) (k4\_rvsum\_1 \\ & X2 X3) = k4\_rvsum\_1 (k8\_rvsum\_1 X0 X2) (k8\_rvsum\_1 X1 X3)))))) \end{aligned}$$