

t9_zf_lang1

(TMb68v7Q8CtMuSbZPmPcaRuBqAAnuwMBsSu)

October 27, 2020

Let $v1_zf_lang : \iota \Rightarrow o$ be given. Let $m2_finseq_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k5_numbers : \iota$ be given. Let $m2_subset_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zf_lang : \iota$ be given. Let $k23_zf_lang : \iota \Rightarrow \iota$ be given. Let $k13_zf_lang : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k24_zf_lang : \iota \Rightarrow \iota$ be given. Let $v8_zf_lang : \iota \Rightarrow o$ be given. Let $k10_zf_lang : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v9_zf_lang : \iota \Rightarrow o$ be given. Let $k11_zf_lang : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v10_zf_lang : \iota \Rightarrow o$ be given. Let $k12_zf_lang : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v11_zf_lang : \iota \Rightarrow o$ be given. Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $m1_finseq_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k4_ordinal1 : \iota$ be given. Let $r1_xreal_0 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $np_5 : \iota$ be given. Assume the following.

$$\begin{aligned}
 & \forall X0.((v1_zf_lang X0) \wedge (m2_finseq_1 X0 k5_numbers)) \Rightarrow ((\\
 & \quad \neg(v8_zf_lang X0) \wedge (\forall X1.((v1_zf_lang X1) \wedge (m2_finseq_1 \\
 & \quad X1 k5_numbers)) \Rightarrow (\forall X2.((v1_zf_lang X2) \wedge (m2_finseq_1 X2 \\
 & \quad k5_numbers)) \Rightarrow (X0 \neq k10_zf_lang X1 X2)))) \wedge (((\exists X1.((v1_zf_lang \\
 & \quad X1) \wedge (m2_finseq_1 X1 k5_numbers)) \wedge (\exists X2.((v1_zf_lang X2) \wedge \\
 & \quad (m2_finseq_1 X2 k5_numbers)) \wedge (X0 = k10_zf_lang X1 X2))) \Rightarrow (v8_zf_lang \\
 & \quad X0)) \wedge ((\neg(v9_zf_lang X0) \wedge (\forall X1.((v1_zf_lang X1) \wedge (m2_finseq_1 \\
 & \quad X1 k5_numbers)) \Rightarrow (\forall X2.((v1_zf_lang X2) \wedge (m2_finseq_1 X2 \\
 & \quad k5_numbers)) \Rightarrow (X0 \neq k11_zf_lang X1 X2)))) \wedge (((\exists X1.((v1_zf_lang \\
 & \quad X1) \wedge (m2_finseq_1 X1 k5_numbers)) \wedge (\exists X2.((v1_zf_lang X2) \wedge \\
 & \quad (m2_finseq_1 X2 k5_numbers)) \wedge (X0 = k11_zf_lang X1 X2))) \Rightarrow (v9_zf_lang \\
 & \quad X0)) \wedge ((\neg(v10_zf_lang X0) \wedge (\forall X1.((v1_zf_lang X1) \wedge (m2_finseq_1 \\
 & \quad X1 k5_numbers)) \Rightarrow (\forall X2.((v1_zf_lang X2) \wedge (m2_finseq_1 X2 \\
 & \quad k5_numbers)) \Rightarrow (X0 \neq k12_zf_lang X1 X2)))) \wedge (((\exists X1.((v1_zf_lang \\
 & \quad X1) \wedge (m2_finseq_1 X1 k5_numbers)) \wedge (\exists X2.((v1_zf_lang X2) \wedge \\
 & \quad (m2_finseq_1 X2 k5_numbers)) \wedge (X0 = k12_zf_lang X1 X2))) \Rightarrow (v10_zf_lang \\
 & \quad X0)) \wedge ((\neg(v11_zf_lang X0) \wedge (\forall X1.(m2_subset_1 X1 k5_numbers \\
 & \quad k1_zf_lang)) \Rightarrow (\forall X2.((v1_zf_lang X2) \wedge (m2_finseq_1 X2 k5_numbers)) \Rightarrow \\
 & \quad (X0 \neq k13_zf_lang X1 X2)))) \wedge (((\exists X1.(m2_subset_1 X1 k5_numbers \\
 & \quad k1_zf_lang) \wedge (\exists X2.((v1_zf_lang X2) \wedge (m2_finseq_1 X2 k5_numbers)) \wedge \\
 & \quad (X0 = k13_zf_lang X1 X2))) \Rightarrow (v11_zf_lang X0)))))))))
 \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(m2_subset_1 X0 k5_numbers k1_zf_lang) \Rightarrow (\forall X1. \\
& ((v1_zf_lang X1) \wedge (m2_finseq_1 X1 k5_numbers)) \Rightarrow (\forall X2.(\\
& (v1_zf_lang X2) \wedge (m2_finseq_1 X2 k5_numbers)) \Rightarrow ((v11_zf_lang \\
& X1) \Rightarrow ((\neg(X0 = k23_zf_lang X1) \wedge (\forall X3.((v1_zf_lang X3) \wedge (m2_finseq_1 \\
& X3 k5_numbers)) \Rightarrow (k13_zf_lang X0 X3 \neq X1))) \wedge ((\exists X3.((v1_zf_lang \\
& X3) \wedge (m2_finseq_1 X3 k5_numbers)) \wedge (k13_zf_lang X0 X3 = X1)) \Rightarrow (X0 = \\
& k23_zf_lang X1)) \wedge ((\neg(X2 = k24_zf_lang X1) \wedge (\forall X3.(m2_subset_1 \\
& X3 k5_numbers k1_zf_lang) \Rightarrow (k13_zf_lang X3 X2 \neq X1))) \wedge ((\exists X3. \\
& (m2_subset_1 X3 k5_numbers k1_zf_lang) \wedge (k13_zf_lang X3 X2 = X1)) \Rightarrow \\
& (X2 = k24_zf_lang X1)))))))))
\end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.((\neg v1_xboole_0 X0) \wedge ((\neg v1_xboole_0 X1) \wedge \\
& (m1_subset_1 X1 (k1_zfmisc_1 X0)))) \Rightarrow (\forall X2.(m2_subset_1 \\
& X2 X0 X1) \Leftrightarrow (m1_subset_1 X2 X1))
\end{aligned} \tag{3}$$

Assume the following.

$$\forall X0.\forall X1.(m2_finseq_1 X1 X0) \Leftrightarrow (m1_finseq_1 X1 X0) \tag{4}$$

Assume the following.

$$k5_numbers = k4_ordinal1 \tag{5}$$

Assume the following.

$$\neg v1_xboole_0 k1_zf_lang \tag{6}$$

Assume the following.

$$m1_subset_1 k1_zf_lang (k1_zfmisc_1 k5_numbers) \tag{7}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.((m1_subset_1 X0 k1_zf_lang) \wedge ((v1_zf_lang \\
& X1) \wedge (m1_finseq_1 X1 k5_numbers))) \Rightarrow ((v1_zf_lang (k13_zf_lang \\
& X0 X1)) \wedge (m2_finseq_1 (k13_zf_lang X0 X1) k5_numbers))
\end{aligned} \tag{8}$$

Assume the following.

$$\begin{aligned}
& k1_zf_lang = ReplSep (toset (\lambda X0 : \iota.m1_subset_1 X0 k5_numbers)) \\
& (\lambda X0 : \iota.r1_xreal_0 np_5 X0) (\lambda X0 : \iota.X0)
\end{aligned} \tag{9}$$

Assume the following.

$$\forall X0.(v1_xboole_0 X0) \Rightarrow (\forall X1.(m1_subset_1 X1 (k1_zfmisc_1 X0)) \Rightarrow (v1_xboole_0 X1)) \tag{10}$$

Theorem 1

$$\begin{aligned}
& \forall X0.((v1_zf_lang X0) \wedge (m2_finseq_1 X0 k5_numbers)) \Rightarrow (\forall X1. \\
& (m2_subset_1 X1 k5_numbers k1_zf_lang) \Rightarrow ((k23_zf_lang (k13_zf_lang \\
& X1 X0) = X1) \wedge (k24_zf_lang (k13_zf_lang X1 X0) = X0)))
\end{aligned}$$